

# SIMULATION AND ANALYSIS OF RAILWAY SYSTEM WITH POWER FLOW CONTROL OF ASYMMETRIC LC COUPLING BRANCHES

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**ABSTRACT :** In this paper the major problem is about power quality and excessive neutral sections of the conventional two-phase electric railway supply system. The best way for adopting railway static power conditioner (RPC) which is depend upon the single-phase supply system which is a feasible solution. Therefore to improve the reliability of RPC and cost-efficiency, a novel compensating system is defined as a asymmetric double LC-coupled railway power flow conditioner (ALC-RPFC) which is introduced in this paper. The study which indicates the comparison between the proposed ALC-RPFC and the conventional RPC which have the effective heavy-load compensating ability with the lower power rating, there is more benefit to improve the converter's operating reliability and efficiency. Therefore the design technique for the LC coupling branches which is developed in this paper which is more suitable for fluctuated railway loads, and which is also used for the implementation of industrial applications. The simulation result demonstrate the good heavy-load compensating performance and power capacity reduce the ability of the ALC-RPFC.

**Index Terms**—Asymmetric LC-coupling branches, electrical railway power system, parameter design, power capacity analysis, power flow control.

## INTRODUCTION

Considering the efficiency, adoption of the phase rotation technique is the most conventional method for electrical railway power system. However, it lacks flexibility and cannot solve all power quality problems. Moreover, these problems will become more prominent in the remote areas with unrobust power system (e.g., mountainous and plateaus areas). Compared to conventional transformers, the balance traction transformer (BTT) can have a better ability of suppressing NSC.

Unfortunately, the ability of BTT to suppress NSC is affected by load variation. Therefore, the three-phase power system can hardly be balanced by this method. Besides, this class of special-type transformer usually contains a complex winding structure, and it is also not beneficial for the elimination of harmonics and reactive power. SCR-controlled static VAR compensator can also be used to compensate NSC and reactive power in traction supply systems. But it is difficult to get a satisfactory state in both technical and economic aspects.

Compared to conventional transformers, the balance traction transformer (BTT) can have a better

ability of suppressing NSC. Unfortunately, the ability of BTT to suppress NSC is affected by load variation. That is to say, the greater imbalance of two-phase loads, the worse ability of NSC suppression. Therefore, the three-phase power system can hardly be balanced by this method. Besides, this class of special-type transformer usually contains a complex winding structure, and it is also not beneficial for the elimination of harmonics and reactive power.

SCR-controlled static VAR compensator can also be used to compensate NSC and reactive power in traction supply systems. But it is difficult to get a satisfactory state in both technical and economic aspects. To overcome the disadvantages, various IGBT- or IGCT based active compensating systems were put forward in the last 20 years. Among them, RPC gets more attention due to its universality. It can deal with almost all power quality problems of two-phase and single-phase traction supply system. However, a relatively high compensation capacity and initial investment slow down its large-scale industrial application.

## TOPOLOGY OF ALC-RPFC SYSTEM

Fig. 1 shows the topology of ALC-RPFC system. The three phase 110 kV (or 220 kV) high voltage grid is stepped down into 27.5-kV single-phase traction network by Ta so as to feed locomotives.

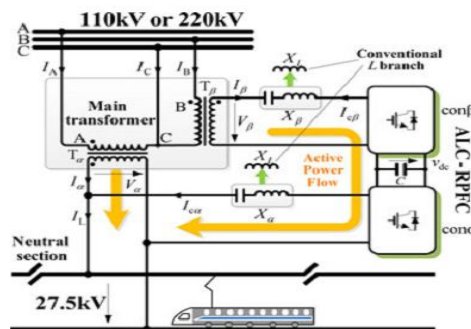


Fig. 1. Topology of ALC-RPFC system.

Fig. 2 shows the equivalent circuit of phase- $\alpha$  and  $\beta$ . Among which,  $V_{ck}$  and  $I_{ck}$  are the fundamental voltage and current of converter  $k$ , respectively;  $X_k$  is the equivalent fundamental reactance and  $V_{Xk}$  the voltage drop of coupling

branch in phase k, respectively;  $V_k$  and  $I_k$  are the secondary voltage and current of  $T_k$ ;  $I_L$  is the load's current ( $k \in \{\alpha, \beta\}$ ).

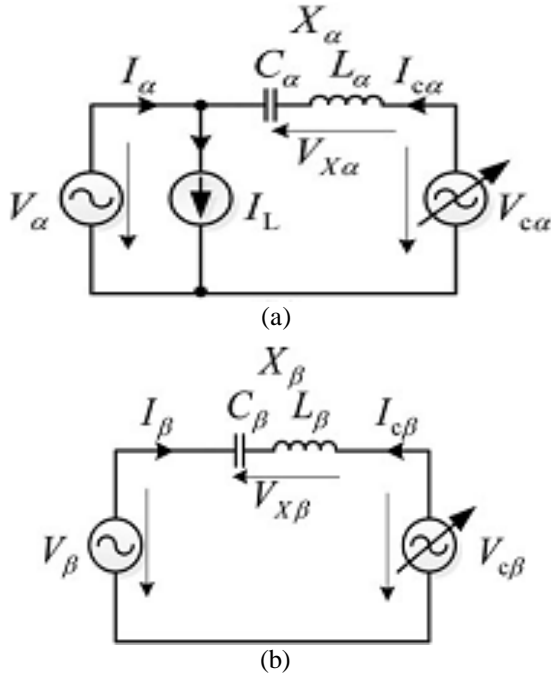


Fig. 2. Equivalent circuits of phase- $\alpha$  and  $\beta$ . (a) Phase- $\alpha$ . (b) Phase- $\beta$

**OPERATING PROPERTY OF ALC-RPFC  
Basic Requirements of Converters**

Ignoring the influences of harmonics and turn's ratio difference between  $T_\alpha$  with  $T_\beta$ ; the phasor diagram of ALC-RPFC is shown in Fig. 3 (Note that the voltages and currents of phase- $\beta$  shown in Fig. 3 are converted to the same level of phase- $\alpha$ ). ALC-RPFC should satisfy the following requirements [7]:

- 1) Transforming half of the load's active power from phase- $\beta$  (EO, i.e.,  $0.5I_Lp$ ) to phase- $\alpha$  (GD, i.e.,  $0.5I_Lp$ ).
- 2) Compensating appropriate leading reactive power for phase- $\alpha$  (BC) and lagging reactive power for phase- $\beta$  (EF).

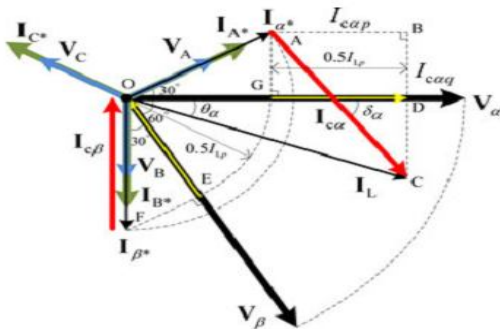


Fig. 3. Compensating phasor diagram of ALC-RPFC system.

Therefore, it can be observed from Fig. 3 that the output currents of  $T_\alpha$  and  $T_\beta$  are converted from  $I_L$  and 0 into  $I_{\alpha^*}$  and  $I_{\beta^*}$ , respectively. The primary three phase currents  $I_{A^*}$ ,  $I_{B^*}$ , and  $I_{C^*}$  inducted by  $I_{\alpha^*}$  and  $I_{\beta^*}$  are balanced as well. Obviously, their PF is 1. Hence, the compensating currents of  $con_\alpha$  and  $con_\beta$  are  $I_{c\alpha}$  and  $I_{c\beta}$ , respectively. By the way, this compensating principle is also useful for RPC [17].

To get the requirements stated previously, referring to Fig. 3,  $\delta_\alpha$  ( $\delta_\alpha = \angle V_\alpha - \angle I_{c\alpha}$ ) and the load's PF,  $\lambda$  ( $\lambda = \cos\theta_\alpha$ ), should satisfy

$$\delta_\alpha = \arctan\left(\frac{I_{c\alpha q}}{I_{c\alpha p}}\right) = \arctan\left(\frac{1}{\sqrt{3}} + 2\sqrt{\frac{1}{\lambda^2} - 1}\right) \quad (1)$$

where  $I_{c\alpha p}$  and  $I_{c\alpha q}$  are the active and reactive part of  $I_{c\alpha}$ , respectively (i.e., AB and BC in Fig. 3). From (1), the relationship of  $\delta_\alpha$  and  $\lambda$  can be obtained as shown in Fig. 4.

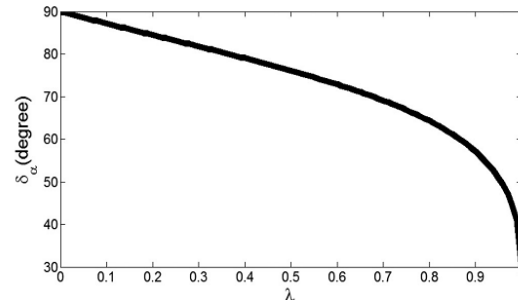


Fig. 4. Curves of  $\delta_\alpha$  ( $\lambda$ ).

Obviously,  $\delta_\alpha$  is in inverse proportion to  $\lambda$ . Besides, the compensating current  $I_{c\alpha}$  of  $con_\alpha$  and load current  $I_L$  should satisfy (2), i.e

$$I_{c\alpha} = I_{c\alpha p}^2 + I_{c\alpha q}^2 = \varepsilon I_L \quad (2)$$

where

$$\varepsilon = \sqrt{-\frac{2}{3}\lambda^2 + \frac{\lambda}{\sqrt{3}}\sqrt{1-\lambda^2} + 1} \quad (3)$$

**Output Voltage of  $con_\alpha$**

From Fig. 2(a),  $con_\alpha$ 's fundamental output voltage,  $V_{c\alpha}$ , can be expressed as

$$V_{c\alpha} = V_\alpha + jX_\alpha I_{c\alpha} = f(V_\alpha, X_\alpha, I_{c\alpha}, \delta_\alpha) \quad (4)$$

where  $X_\alpha = \omega L_\alpha - 1/\omega C_\alpha$  is the LC branch's fundamental reactance of phase- $\alpha$ ;  $\delta_\alpha$  is the phase difference between  $V_\alpha$  and  $I_{c\alpha}$ ;  $f(*)$  represents a function of  $V_\alpha$ ,  $X_\alpha$ ,  $I_{c\alpha}$ , and  $\delta_\alpha$ .

For an electric railway supply system, the normal voltage of  $V_\alpha$  is a constant, while  $X_\alpha$  will be discussed in the next section.

Situation 1: The phase of  $I_{c\alpha}$  is constant (i.e.,  $\delta_\alpha$  unchanging), but its amplitude variable. Fig. 5 shows the phasor diagram of  $con_\alpha$ 's output voltage ( $X_\alpha < 0$ ) when  $\delta_\alpha$  is constant. It can be seen from Fig. 5 that the terminal point of  $V_{c\alpha}$  shifts in the vertical line of  $I_{c\alpha}$  ( $V_{c\alpha 1} \rightarrow V_{c\alpha m} \rightarrow V_{c\alpha 2}$ ) when  $I_{c\alpha}$  varies along with  $L_2$  ( $I_{c\alpha 1} \rightarrow I_{c\alpha} \rightarrow I_{c\alpha 2}$ ). The minimum value of  $V_{c\alpha}$ ,  $V_{c\alpha m}$ , precisely appears in the intersection point of  $L_1$  and  $L_2$  (i.e., point D).

$$\begin{cases} V_{cam} = V_{\alpha} \cos \delta_{\alpha} \\ |X_{am}| = \frac{1}{\omega C_{\alpha}} - \omega L_{\alpha} = \frac{V_{\alpha} \sin \delta_{\alpha}}{I_{ca}} \end{cases} \quad (5)$$

where  $X_{am}$  is the LC branch's fundamental reactance of phase-  $\alpha$  when  $V_{ca} = V_{cam}$ . Because  $\delta_{\alpha} \in [30^{\circ}, 90^{\circ}]$  (see Fig. 4), it can be calculated from (5) that  $V_{cam} \in [0, 0.866V_{\alpha}]$ . That is to say, no matter the changes of  $I_{ca}$ 's phasor angle,  $V_{cam}$  is always less than  $V_{\alpha}$ , and its maximum value is only  $0.866V_{\alpha}$ .

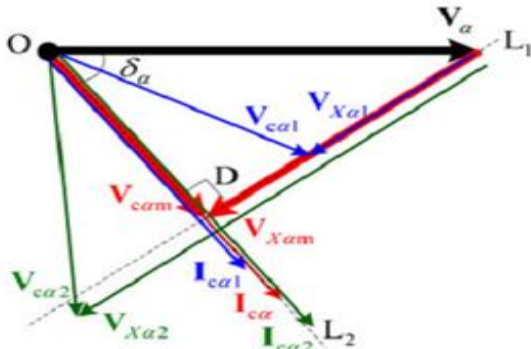


Fig. 5. Phasor diagram of  $con_{\alpha}$  when  $\delta_{\alpha}$  is constant.

1) Situation 2: The amplitude of  $I_{ca}$  is constant, but its phase variable (i.e.,  $\delta_{\alpha}$  variable). Fig. 6 shows the phasor diagram of  $con_{\alpha}$  when  $I_{ca}$  is a constant ( $X_{\alpha} = X_{am} < 0$ ). The variables shown in Fig. 6 satisfy the following relationship:

$$\begin{cases} I'_{ca} = I_{cam} = I_{ca} \\ V'_{X\alpha} = V_{Xam} = V_{X\alpha} \\ \delta'_{\alpha} > \delta_{am} > \delta_{\alpha} \\ V'_{ca} = V_{cam} = V_{ca} \end{cases} \quad (6)$$

It can be seen from Fig. 6 that the smaller the phase angle between  $V_{\alpha}$  with the compensating current (i.e.,  $\delta_{\alpha} < \delta_{am} < \delta_{\alpha}'$ ), the larger the output voltage of  $con_{\alpha}$  (i.e.,  $V_{ca} > V_{cam} > V_{ca}'$ ).

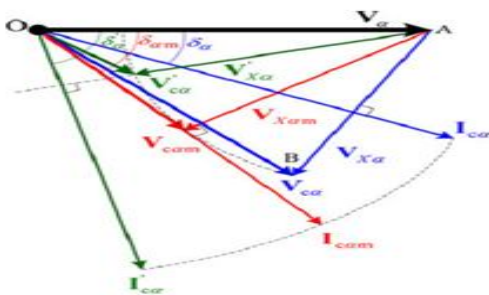


Fig. 6. Phasor diagram of  $con_{\alpha}$  when  $I_{ca}$  is constant.

### PARAMETER DESIGN AND SYSTEM CONTROL BASED ON THE FLUCTUATED LOAD CONDITION

#### Parameter Design of Phase- $\alpha$

##### 1) Synergetic Design Principle Between $X_{\alpha}$ With $con_{\alpha}$ :

It can be deduced from the previous discussions that  $X_{\alpha}$  is a key parameter of ALC-

RPFC, which has significant influence for the output performance of the power conditioner. To give an optimal balance between compensating performance and cost efficiency, we will give a synergetic design guideline for  $X_{\alpha}$  and  $con_{\alpha}$ :

a) When the traction supply system operates in the heavy load situation, the output voltage of  $con_{\alpha}$  should be as low as possible. It allows ALC-RPFC to get the satisfactory heavy-load compensating ability with lower voltage rating and switching frequency.

b) In the premise of satisfying the first designing principle, an appropriate  $X_{\alpha}$  should also make the apparent power of the converter as high as possible. In this way, the power capacity utilization rate of the compensating system can be increased.

In the typical variation range of load currents, the designed  $X_{\alpha}$  should make the compensating system to have the obvious economic advantage than conventional RPC.

#### 2) Designing Idea of $X_{\alpha}$ :

a) **Realization of the first design principle:** In order to meet the first designing principle, the second term of (5) seems to be an available method. Unfortunately, the load working condition in the real traction network is much complex, so that it is difficult to estimate.

Fig. 7 shows the phasor diagram of ALC-RPFC at four typical working conditions, in which,  $I_{ca}$ ,  $I_{ca}'$ ,  $I_{cam}$ , and  $I_{cam}'$  are the corresponded four compensating currents of  $con_{\alpha}$ , and satisfying  $I_{ca} = I_{ca}' < I_{cam} = I_{cam}'$ . Considering  $\delta_{\alpha} \in [30^{\circ}, 90^{\circ}]$  (see Fig. 4), it can be deduced from Fig. 7 that  $30^{\circ} \leq \delta_{am} \leq \delta_{\alpha} \leq 90^{\circ}$ .

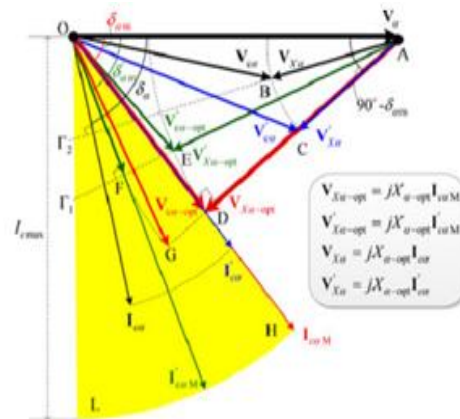


Fig. 7. Phasor diagram of ALC-RPFC in the variable load condition.

From Fig. 7, it can be concluded that, no matter how the railway load changes, all the compensating currents are located in the yellow fan-shaped area of OHL. Therefore,  $I_{ca}$  and  $I_{ca}'$  are the representative compensating currents of  $con_{\alpha}$  when their amplitudes is less than  $I_{cam}$ . While  $I_{cam}$  and  $I_{cam}$  are the representative ones when  $con_{\alpha}$ 's



compensating currents is equal to  $I_{cmax}$ . Besides, we must emphasize here that the load's PF is not a fixed value in both of those two cases; it changes the value along with  $\delta\alpha$ . Additionally, when the compensating current equals  $I_{cmax}$ , a suitable  $X\alpha$  should make  $con\alpha$  operate at the minimal output voltage, e.g., OD and OF shown in Fig. 7. Because selecting the minimal output voltage as the normal voltage, a minimal apparent power can be obtained.

In the following, we will select an optimal one in those two representative cases:

1) If  $\Delta ADO$  is adopted to design  $X\alpha$ , it can be seen from Fig. 7 that when the compensating current changes from the normal current  $I_{cam}$  to another normal one  $I_{cam}'$ , the output voltage of  $con\alpha$  will transform from OD to OE. Obviously  $OE < OD$ , which means, when the compensating current shifts along with arc HL, adopting  $\Delta ADO$  to design  $X\alpha$ ,  $con\alpha$ 's output voltage will not exceed OD.

2) If  $\Delta AFO$  is adopted to design  $X\alpha$ , similarly, when the compensating current changes from the normal current  $I_{cam}$  to another normal current  $I_{cam}'$ , the output voltage of  $con\alpha$  will transform from OF to OG. Hence, to get the minimal output voltage and apparent power of  $con\alpha$  in the condition of load changes (i.e., the first design principle), select  $\Delta ADO$  to design  $X\alpha$  is better than others. From  $\Delta ADO$ , the optimal  $|X\alpha|$ ,  $|X\alpha-opt|$ , can be calculated by

$$|X_{\alpha-opt}| = \frac{AD}{I_{c\alpha M}} = \frac{V_{X\alpha-opt}}{I_{c\alpha M}} = \frac{V_{\alpha} \sin \delta_{\alpha m}}{I_{c\alpha M}} \quad (7)$$

where  $I_{c\alpha m}$  is the maximum value of  $I_{c\alpha}$ ;  $\delta_{\alpha m}$  is the minimum compensating current angle of  $con\alpha$ , and it satisfies [see (1)]

$$\delta_{\alpha m} = \arctan\left(\frac{1}{\sqrt{3}} + 2\sqrt{\frac{1}{\lambda_{max}^2} - 1}\right) \quad (8)$$

where  $\lambda_{max}$  is the maximum PF of load current.

**b) Verification of the second design principle:** Referring to Fig. 7, when  $I_{cam}$  (normal current) decreases to  $I_{ca}'$ ,  $\Delta ADO$  degenerates into  $\Delta ACO$ , and the output voltage of  $con\alpha$ , however, increases from  $V_{c\alpha-opt}$  (i.e., OD) to  $V_{c\alpha}'$  (i.e., OC)

The terminal point of  $V_{c\alpha}$  (point B) in  $\Delta ABO$  (the most ordinary working condition of  $con\alpha$ ) has to be constrained shifting in line AD, can the maximum value of  $S_{c\alpha}$  (the apparent power of  $con\alpha$ ) may be obtained. In this case,  $I_{ca} \rightarrow I_{ca}'$ ,  $\Delta ABO \rightarrow \Delta ACO$ .

From  $\Delta ACO$ ,  $S_{c\alpha}$  can be calculated by

$$S_{c\alpha} = I_{c\alpha} V_{c\alpha}'$$

$$= I_{c\alpha} \sqrt{V_{\alpha}^2 + I_{c\alpha}^2 X_{\alpha-opt}^2 - 2I_{c\alpha} |X_{\alpha-opt}| V_{\alpha} \sin \delta_{\alpha m}} \quad (9)$$

Note that because  $\Delta ABO \Delta ACO$ ,  $I_{ca}'$  is substituted by  $I_{ca}$  in (9). Fig. 8 shows the relationship among  $S_{c\alpha}$ ,  $I_{ca}$ , and  $\lambda_{max}$ , which is obtained by the per-unit expression of (9)

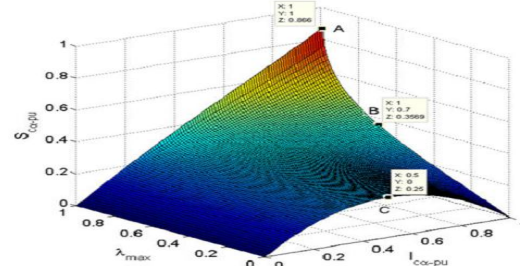


Fig. 8. Relationship among  $S_{c\alpha}$ ,  $I_{c\alpha}$ , and  $\lambda_{max}$  (Note that the base values are selected as  $V_B = V_{\alpha}$ ,  $I_B = I_{c\alpha M}$ .)

**2) Calculating Method of  $X\alpha-opt$  for Practical Application:** Because  $I_{c\alpha}$  cannot be measured directly, (7) is not a convenient calculating method for practical application. The following, we will give a useful one for designing  $X\alpha-opt$ . The curve of  $\varepsilon(\lambda)$  is shown in Fig. 9 [originate from (3)]. Usually, the probability of locomotives' PF locates in 0.7~0.9 is much higher than other values. While, it can be observed from Fig. 9 that when  $\lambda \in [0.7, 0.9]$ ,  $\varepsilon(\lambda)$  locates in a narrow interval of 0.8285~0.9808, which means  $I_{c\alpha}$  is approximately proportional with IL.

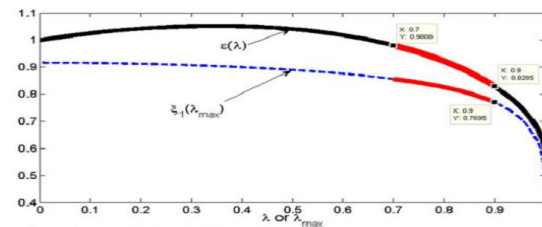


Fig. 9. Curves of  $\varepsilon(\lambda)$  and  $\xi_1(\lambda_{max})$ .

So, referring to (2),  $I_{c\alpha m}$  can be approximately expressed as

$$I_{c\alpha M} \approx \frac{I_{LM}}{0.2} \int_{0.7}^{0.9} \varepsilon(\lambda) d\lambda = \varepsilon_{aver} I_{LM} = 0.916 I_{LM} \quad (10)$$

where  $I_{LM}$  is the maximum value of IL,  $\varepsilon_{aver}$  is the average value of  $\varepsilon$  when  $\lambda \in [0.7, 0.9]$ .

Remark 1: For different electrical railway power system, the load's PF may not accurately distributes in 0.7~0.9, so it is better to modify  $\varepsilon_{aver}$ 's value flexibly based on the form shown in (10), by applying the real statistic result of  $\lambda$  in practical applications. Substituting (10) and (8) into (7), the final practical used expression of  $|X\alpha-opt|$  can be expressed as

$$|X_{\alpha-opt}| = \frac{1}{\omega C_{\alpha}} - \omega L_{\alpha} = \xi_1 \frac{V_{\alpha}}{I_{LM}} \quad (11)$$

Where

$$\xi_1 = \varepsilon_{aver} \frac{\lambda_{max}/\sqrt{3} + \sqrt{1 - \lambda_{max}^2}}{\sqrt{\frac{2}{3}\lambda_{max}^2 + \frac{\lambda_{max}}{\sqrt{3}}\sqrt{1 - \lambda_{max}^2} + 1}} \quad (12)$$

For the consideration of designing convenience, the curve of  $\xi_1(\lambda_{max})$  is also given in Fig. 9 (dotted line). The concept of 95%-probability

value is always be used in practical cases, so (11) can be also rewritten as

$$|X_{\alpha-opt}| = \frac{1}{\omega C_{\alpha}} - \omega L_{\alpha} = \xi_1 |\lambda_{max} = \lambda_{95\%(U)} \frac{V_{\alpha}}{I_{L-95\%(U)}} \quad (13)$$

where  $\lambda_{95\%(U)}$  and  $IL-95\%(U)$  are the upper-95%-probability value of  $\lambda$  and  $IL$ , respectively.

**Parameter Design of Phase- $\beta$**

Fig. 10 shows the phasor diagram of phase- $\beta$ , in which,  $\Delta ADO$  is the voltage triangle of  $\text{con}\alpha$ , and it is the same with  $\Delta ADO$  shown in Fig. 7.  $I_{c\beta M}$  is the maximum compensating current phasor of  $\text{con}\beta$ , and it leads  $V_{\alpha}$   $90^{\circ}$ .  $V_{c\beta M}$  is the maximum output voltage of  $\text{con}\beta$ .  $V_{\beta}$  lags  $V_{\alpha}$   $60^{\circ}$ .

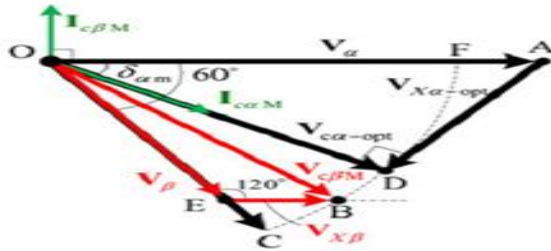


Fig. 10. Phasor diagram of phase- $\beta$ .

In order to reduce the cost, improve the reliability of converters and design flexibility of the coupling branch, it is reasonable to make  $X_{\beta}$  meet the following design principles:

- 1) It is better to make  $V_{c\beta M} = V_{c\alpha-opt}$  when the compensating current of  $\text{con}\alpha$  reaches its maximum value  $I_{c\alpha m}$ .
- 2) In the premise of avoiding large inductance, designers should have sufficient flexibility to match the parameters of coupling branch when  $V_{\beta}$  is a fixed value (it often happens in the renovation projects).

The typical voltage triangle of  $\text{con}\beta$  in Fig. 10 is  $\Delta BEO$ , where

$$\begin{cases} V_{\beta} = OE = \tau V_{c\alpha-opt}, 0 < \tau < 1 \\ V_{X\beta} = EB = |X_{\beta}| I_{c\beta M} \\ V_{c\beta M} = OB = OD = V_{c\alpha-opt} \end{cases} \quad (14)$$

in which  $EB$  is the voltage drop of the LC-coupling branch,  $X_{\beta}$  is the fundamental reactance of the LC branch of phase- $\beta$ . Besides,  $V_{\beta}$  should be designed less than  $V_{c\alpha-opt}$  (i.e.,  $V_{\beta} = \tau V_{c\alpha-opt}$ ,  $0 < \tau < 1$ ). Referring  $\Delta ADO$  in Fig. 10, and combine (14) and (7)–(12), it can be calculated that

$$\begin{aligned} V_{\beta} &= \tau \sqrt{V_{\alpha}^2 - V_{X\alpha-opt}^2} \\ &= \frac{\tau \lambda_{max}}{2 \sqrt{\frac{2}{3} \lambda_{max}^2 + \frac{\lambda_{max}}{\sqrt{3}} \sqrt{1 - \lambda_{max}^2} + 1}} V_{\alpha} \end{aligned} \quad (15)$$

Considering that when  $I_{c\beta} = I_{c\beta M}$ , the active part of  $IL$ ,  $I_{Lp}(IL_p = \lambda IL)$ , bound to reach its maximum value, so  $I_{c\beta M}$  can be easily calculated by the current relationship shown in Fig. 3, i.e.

$$I_{c\alpha\beta M} = \frac{N I_{LM} \lambda_{max}}{2 \cos 30^{\circ}} = N \frac{I_{LM} \lambda_{max}}{\sqrt{3}} \quad (16)$$

where  $N = V_{\alpha} / V_{\beta}$ . By using the cosine theorem in  $\Delta BEO$  (see Fig. 10) and combining (14)–(16),  $|X_{\beta}|$  can be calculated by

$$|X_{\beta}| = \frac{1}{\omega C_{\beta}} - \omega L_{\beta} = \xi_2 \frac{V_{\alpha}}{I_{LM}} \quad (17)$$

Where

$$\xi_2 = \frac{\sqrt{3}\tau(4-3\tau^2-\tau)\cos^2\delta_{am}}{2\lambda_{max}}, 0 < \tau < 1 \quad (18)$$

Similar to design  $X_{\alpha}$ , instead of  $\lambda_{max}$  and  $ILM$ ,  $\lambda_{95\%(U)}$  and  $IL-95\%(U)$  can also be used in (15) and (17), (18) to calculate  $V_{\beta}$  and  $X_{\beta}$  in practical applications.

The design curve of  $L_{\beta}$  and  $C_{\beta}$  can be easily obtained from (17) and a real design example is shown in Fig. 17 of Section VI, which can be used to flexibly configure  $L_{\beta}$  and  $C_{\beta}$  according to the actual situation. For convenience of design, Fig. 11 gives the design surface of  $\xi_2$ .

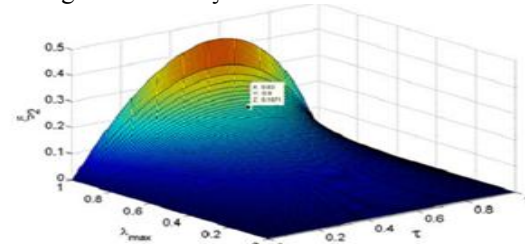


Fig. 11. Design surface of  $\xi_2$ .

**Control System of Low-Rated Laboratory Model**

Fig. 12 shows the control diagram of a low-rated ALC-RPFC. Based on the Fourier transformation theory, it can be verified that the output signal of low passive filter is  $IL_p/\sqrt{2}$  ( $IL_p$  is the active part of  $IL$ ) [17].  $i_{\alpha}^*$  and  $i_{\beta}^*$  are the expected output currents of  $T_{\alpha}$  and  $T_{\beta}$ , respectively. For the consideration of resonance, when the control method shown in Fig. 12 is adopted, ALC-RPFC can be equivalent to an active filter with infinite harmonic damping factor in harmonic frequencies, so the harmonic resonance can be suppressed effectively

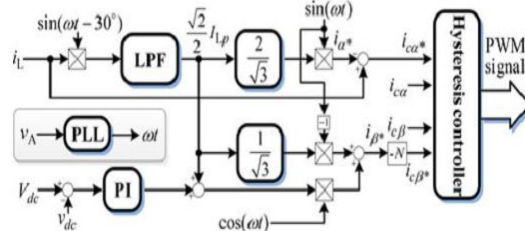


Fig. 12. Control diagram of low-rated ALC-RPFC  
**POWER CAPACITY ANALYSIS AND DC-LINK VOLTAGE DESIGN**

For the same compensating task, ALC-RPFC and RPC have the same compensating currents, so the converters' power ratings of two systems are mainly decided by the output voltage of

con $\alpha$  [26], [27]. More accurately to say, is the dc-link voltage

**Proposed ALC-RPFC**

It can be observed from  $\Delta$ ACO in Fig. 7 that, when  $I_{ca}'$  increases to  $I_{cam}$ ,  $V_{X\alpha}' \rightarrow V_{X\alpha-opt}$ , then con $\alpha$ 's output voltage,  $V_{ca}'$ , trends to its minimum value  $V_{ca-opt}$ . In addition, it can also be observed from  $\Delta$ AEO of Fig. 7 that when  $I_{cam} \rightarrow I_{cam}$ ,  $\delta_{am} \rightarrow \delta_{am}'$ , which means the PF becomes smaller.

**Conventional RPC**

For RPC, the situation is reversed. It can be seen from Fig. 13 that, when  $I_{ca}$  increases, the converter's output voltage  $V_{caL}$  of RPC (i.e., OB) will be much larger than  $V_{\alpha}$  (i.e., OA). That is to say, the dc-link voltage of RPC has to be designed much higher than  $\sqrt{2}V_{\alpha}$ .

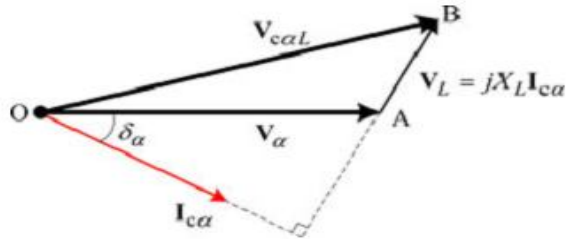


Fig. 13. Phasor diagram of RPC.

From Fig. 13,  $V_{caL}$  can be easily obtained from  $\Delta$ ABO, i.e.

$$V_{caL} = \sqrt{V_{\alpha}^2 + I_{ca}^2 X_L^2 + 2I_{ca} X_L V_{\alpha} \sin \delta_{\alpha}} \quad (19)$$

where  $X_L$  is the reactance of the coupling inductance of RPC. Let  $X_L = \xi |X_{\alpha-opt}|$ , ( $\xi > 0$ ), and considering (7), the perunit form of (19) can be calculated by

$$V_{caL-pu} = \sqrt{(\xi I_{ca-pu} \sin \delta_{am})^2 + 2\xi I_{ca-pu} \sin \delta_{am} \sin \delta_{\alpha} + 1} \quad (20)$$

where the subscript "pu" represents the per-unit form of each variable. then  $\xi \in [0.45, 0.55]$  (Section VI shows a practical designing example of  $X_{\alpha}$ , in which  $|X_{\alpha-opt}| = 46.9\Omega$ ). Let  $\xi = 0.5$  and  $\lambda_{max} = 0.9$  (i.e.,  $\delta_{am} = 57.1$ , because the probability of PF's upper-95%-probability value of locomotives distributes within 0.85~0.93 is much higher than other values), the 3-D plot of  $V_{caL}$  can be obtained from (20), and is shown in Fig. 14.

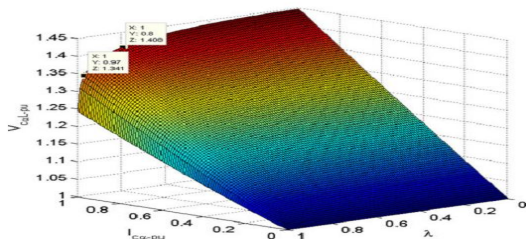


Fig. 14. 3-D plot of  $V_{caL}$  -pu (Note that the base values are  $V_B = V_{\alpha}$ ,  $I_B = I_{caM}$ ).

It can be seen from Fig. 14 that when  $\lambda = 0.8$  (the typical PF of ac-dc locomotives) and  $I_{ca} = 1.0$  p.u.,  $V_{caL}$  reaches its maximum value  $1.408V_{\alpha}$ . So the dc-link voltage of RPC  $V_{dc-L}$  has to be designed to the peak value  $\sqrt{2}V_{caL}$  without consideration of harmonics compensation, i.e.,  $V_{dc-L} \approx 2V_{\alpha}$ .

**SIMULATION RESULT**

The specifications of load currents adopted in the simulation are listed in Table I (measured data), in which,  $i_{L\alpha 1}$  and  $i_{L\alpha 2}$  are adopted to simulate the light (close to  $I_L-95\%(L)$ ) and middle-load working conditions of the TSS, respectively.

Table I  
Specifications Of Load Currents

	RMS/A	1th/A	3th/A	$\lambda$	THD%
$i_{\alpha L1}$	206.4	203.0	32.4	0.805	18.19
$i_{\alpha L2}$	314.4	312.7	57.0	0.746	20.57
$i_{\alpha L1} + i_{\alpha L2}$	524.3	514.9	89.4	0.812	19.16

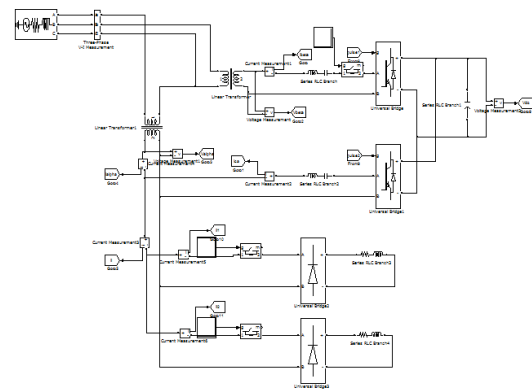


Fig.15 Block diagram of simulation.

Besides,  $i_{L\alpha 1} + i_{L\alpha 2}$  is adopted to simulate the heavy-load situation (close to  $I_L-95\%(U)$ ). The simulating waveforms are shown in Figs. 16–21.

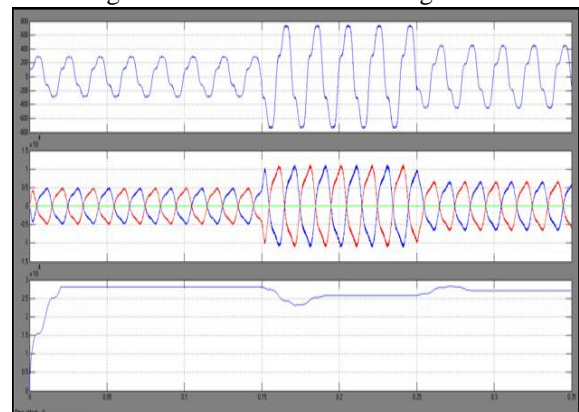


Fig. 16. Simulation waveforms without compensation. (a) Load currents. (b) Primary three phase currents. (c) Feeder voltage's RMS value of phase- $\alpha$ .



Compared with the uncompensated waveforms shown in Fig. 16, it can be observed from It validates the good compensating performance of RPC and ALC-RPFC; although the harmonic compensating performance of RPC is slightly worse than that of ALC-RPFC in the heavy-load case [see Fig. 17 (b)].

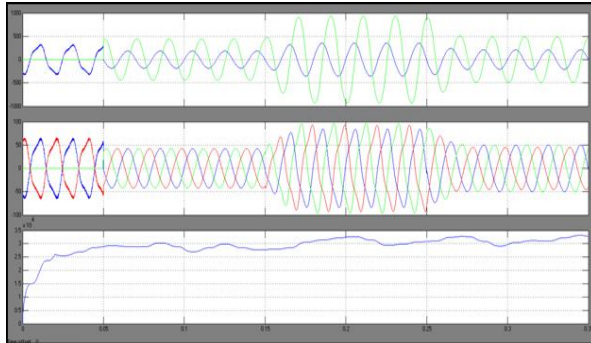


Fig. 17. Simulation waveforms of RPC system when  $V_{dc-L} = 66.7$  kV. (a) Secondary output currents of main transformer. (b) Primary three phase currents. (c) Feeder voltage's RMS value of phase- $\alpha$ .

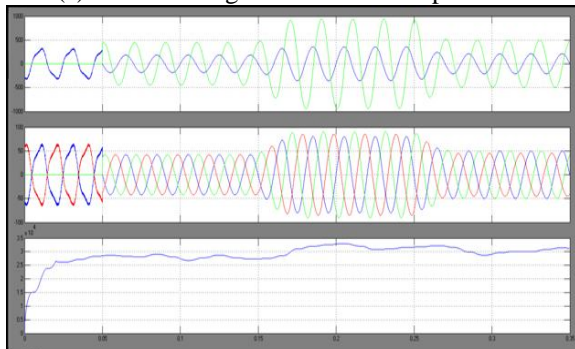


Fig. 18. Simulation waveforms of ALC-RPFC system when  $V_{dc-LC} = 38.9$  kV. (a) Secondary output currents of main transformer. (b) Primary three phase currents. (c) Feeder voltage's RMS value of phase- $\alpha$ .

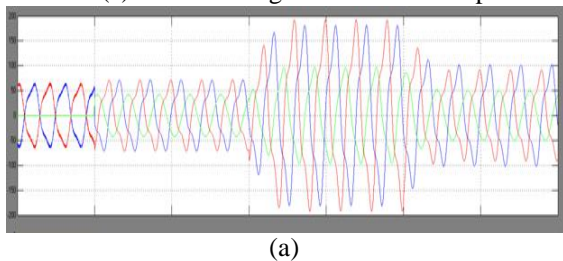


Fig. 19. Simulation waveforms of RPC and ALC-RPFC when the dc-link voltages decrease. (a) Primary three phase currents of RPC when  $V_{dc-L} = 58$  kV.

It can be seen from Fig. 20(a) and (b) that, the conventional RPC shows a worse heavy-load compensating performance when  $V_{dc-L}$  decreases 13% (i.e.,  $V_{dc-L} = 58$  kV). However, when  $V_{dc-LC}$  decreases from 38.9 to 38.3 kV, ALC-RPFC's compensating performance is almost unchanged in

heavy-load working condition [see Fig. 20(c) and (d)].

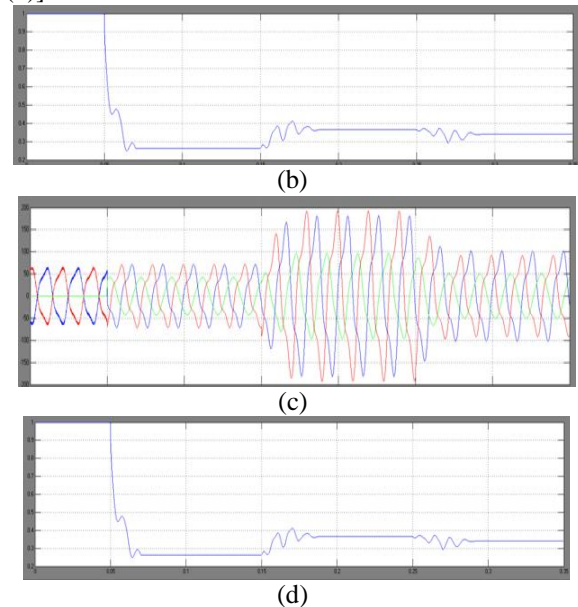


Fig. 20. Simulation waveforms of RPC and ALC-RPFC when the dc-link voltages decrease (b) Unbalance factor of primary three phase currents of RPC system when  $V_{dc-L} = 58$  kV. (c) Primary three phase currents of ALC-RPFC when  $V_{dc-LC} = 38.3$  kV. (d) Unbalance factor of primary three phase currents of ALC-RPFC system when  $V_{dc-LC} = 38.3$  k

## CONCLUSION

The proposed of an asymmetric double LC-coupled with railway power conditioner for a single-phase ac electric railway supply system is present in this paper. For the first time, its operating property undergoes the fluctuated load condition which is analyzed and explained in detailed. Therefore to reach the demand of applications form the "intense and random" load of the electrical railway power system, therefore here we are proposed a systematic design technique for LC-coupling branches, and also the power capacity analysis technique for the purpose of determining the design range of ALC-RPFC's dc-link voltage. At last the simulation results validate these conceptions. ALC-RPFC fully explores the potentials of two asymmetric passive LC branches. When comparison with the conventional RPC, it may have the excellent heavy-load compensating ability with lower dc-link voltage. Besides, all the parameters' design methods proposed in this paper are based on the fluctuated electrical railway working condition, and they are also useful for industrial applications. Therefore, the proposed conditioner is an industrial effective electric railway compensating system with high reliability and high cost-efficiency .

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